The didjeridu (or didgeridoo or yidaki), a musical instrument originally played in parts of Northern Australia, is unusual in the extent to which standing waves in the bore and the player's vocal tract are coupled. Skilled players use resonances of the vocal tract to modify the spectral envelope of the output sound, which gives the instrument its unique timbre. The central bore of these instruments is largely produced by termites eating out the interior of small eucalypt trees. This produces a highly irregular and somewhat flared bore, both of which features are important to the performance quality of the instrument. Occasionally a forked section of a tree is suitably eaten by termites. This allows the manufacture of a 'forked didjeridu' or 'didjeriduo' with a branched bore and two available mouthpieces. It is then possible for a single player to produce changes in pitch and timbre, either by adjusting their lip tension to select different bore resonances, or by using the heel of his hand to close the other mouthpiece. It is even possible for two players to play the same instrument simultaneously. Here we present detailed measurements of the acoustic input impedance of a forked didjeridu. Numerical modelling suggests how the presence of a branched duct might alter the perceived quality of an instrument.

1. INTRODUCTION

The didjeridu (or didgeridoo) is an onomatopoeic English name for a musical instrument originally developed by the indigenous peoples of Northern Australia, where its tribal names include the yidaki, yiragi and mago. It is basically a simple wooden tube with a central bore that is largely produced by termites eating out the interior of small eucalypt trees [1]. The instrument usually plays only a single note at a frequency close to the lowest resonance, although overblowing at the second (and occasionally third) resonance, is used for a musical accent [2-4]. The player places his lips at the narrower end of the tube and uses the technique of ‘circular breathing’ to play continuously. The musical interest comes from the rhythmic contrasts in timbre between the sounds produced during inhalation (during which air from the cheeks is expelled into the instrument) and exhalation.
Unlike other wind instruments, the didjeridu bore lacks a significant restriction at the mouthpiece and consequently an unusually strong coupling can exist between the standing waves in the instrument bore and the player's vocal tract. This allows a skilled player to modify the spectral envelope of the output sound by varying the resonances of his vocal tract [5-7]. The central bore is highly irregular and somewhat flared, both of which features are important to the performance quality of the instrument [8].

Occasionally, a forked section of a tree is suitably eaten by termites. This allows the manufacture of a 'forked didjeridu' or 'didjeriduo' with a branched bore and two available mouthpieces as shown in figure 1. This can be played normally by a single player with the other mouthpiece left open. However, the player can use the heel of his hand to close the other mouthpiece and produce changes in pitch and timbre.

Compared with a normal didjeridu, adding the second branch, whether open or closed, adds new resonances. The musical implications of this are important: adding one or more extra resonance(s) in the lowest range means that the instrument could play two or three pedal notes, instead of one. Adding extra resonances in the higher range, especially in the range 1-2 kHz, can influence the musical performance in a subtle but more important way. It is in this range that the variable, strong formants or enhanced frequency bands are produced by the variations in the player's vocal tract. We have recently shown that properties of the instrument's resonances in this frequency range are among the most important determinants of the perceived quality of an instrument [8].

An unusual feature of some forked didjeridus is that they may be played simultaneously by two players – for novelty value, rather than intrinsic musical interest. Generally this requires that the two bores are joined in the output half of the instrument. If the bores are joined too close to the mouthpieces, it can be difficult for each player to maintain stable lip vibration whilst the bore immediately outside his lips is pressurised by the other player.

In this paper, we present detailed measurements of the acoustic input impedance of a forked didjeridu. Numerical modelling suggests how the presence of a branched duct might alter the perceived quality of an instrument.

Figure 1. The forked didjeridu measured in this study. Tube A is at the top and has an identifying label attached.
2. MATERIALS AND METHODS

The instrument used was made available from the collection of the Didjshop (www.didjshop.com). The input impedance $Z_{in}$, i.e. the impedance at each mouthpiece, was measured as a function of frequency $f$ for each instrument using an impedance spectrometer described in detail elsewhere [9]. Briefly, a waveform is synthesised from harmonic components, amplified and input via a loudspeaker and impedance matching horn to a waveguide of known geometry with three microphones. For these measurements, the spectrometer was calibrated by connecting this waveguide to two reference impedances. One reference was an acoustic open circuit – a rigid seal located at the measurement plane. The other reference was an acoustically quasi-infinite cylindrical pipe (internal diameter = 26.2 mm and length = 194 m) whose impedance was assumed to be real and equal to its calculated characteristic impedance. The spectrometer was then connected to the impedance to be measured, and the unknown impedance spectrum calculated from the pressure components measured in the measurement and two calibration stages. More details are available elsewhere [8]. The subjective parameter overall quality of this instrument was assessed by 6 players giving an average score of 6.1/10 (see [8] for more details, including the relation between subjective quality and physical properties of an instrument). This assessment might be influenced by the higher sound level at the player’s ear when the second tube was open.

3. NUMERICAL MODELLING

A simple one–dimensional model composed of three cylindrical elements was used (see figure 2). The bore of an instrument made by termites in the traditional manner is, of course, very much more complicated. The various impedances were calculated in the standard manner (e.g. see [10]). Radiation impedances were included when appropriate. The values used to approximate the dimensions for the forked didjeridu studied here were: $L_A = 0.93$ m, $L_B = 0.88$ m, $L_C = 0.17$ m, $d_A = d_B = 0.025$ m, $d_C = 0.05$ m.

![Schematic diagram used for a general numerical model of the forked didjeridu. Although the diameter $d_C$ is shown greater than $d_A + d_B$ in this sketch, this is not necessarily true in the model.](image)

4. RESULTS AND DISCUSSION

4.1 Acoustic impedance spectra.

The acoustic impedance spectra, $Z_{in}(f)$ are shown in figure 3, measured for the four possible playing configurations (A or B used as mouthpiece, and in each case with the other port closed or open). As might be expected, the impedance spectra are rather more complicated than those of simple didjeridus [8]. We consider the low frequency behaviour first.
All four configurations display the strong fundamental resonance of frequency $f_1$ required to set up a stable, low frequency oscillation in conjunction with the lips (see figure 4 with an expanded scale at low frequencies). However, an interesting feature is a splitting of the low frequency maxima into a doublet when the other mouthpiece is closed. Figure 4 indicates it is possible to play notes corresponding to each of these adjacent maxima, but we found the lower frequency note to be stronger and easier to play. In each of the four possible configurations, it was possible to play the first overtone at frequency $f_2$. The ratio $f_2/f_1$ lay in the range 2.83 to 2.93. (Indeed skilled players can play both notes in the first overtone doublet that occurs when the other mouthpiece is closed).

We now turn to the critical range 1-2 kHz. In this range, the resonances of a skilled player's vocal tract can attenuate the radiated power over certain frequency ranges. The remaining frequency bands or formants give the instrument characteristic timbres, and it is the variation of these formants over time that is one of the most important elements of idiomatic performance.

The resonances of the tract give rise to peaks in acoustical impedance that are typically one to several MPa s m$^{-3}$ [5,6]. In another study [8], we showed that the most important single determinant of the subjective judgment of instrument quality was the value of $Z_{IN}$ in the frequency range 1 to 2 kHz, with low maximum values associated with high quality instruments. This is readily understood: if the instrument's resonances in this frequency range are too strong, the player is less able to manipulate the spectral envelope with his own resonances.

Figure 3. The measured acoustic input impedance $Z_{IN}$ as a function of frequency plotted on a semi-logarithmic scale for the 4 possible input configurations of the forked didjeridu shown in figure 1. The horizontal dashed lines indicate impedance levels of 0.1 and 1 MPa s m$^{-3}$. 
This instrument could be blown at either tube A or tube B, but tube A was chosen by the Didjshop to be the normal mouthpiece. Figure 3 shows that tube A has the lowest values of $Z_{IN}$ in the frequency range 1 to 2 kHz, particularly when the other tube is open (tube A blown and tube B open). When tube B is closed (tube A blown and tube B closed), there is an increase in the maxima in the 1 to 2 kHz frequency range. This would be expected to alter the timbre of the sound, and to reduce the influence of the player’s vocal tract. A similar increase of $Z_{IN}$ is apparent when tube B is blown and tube A is changed from open to closed.

Inspection of these curves suggests that the low value of $Z_{IN}$ in figure 3 for tubes A and B open is due to cancellation of standing waves. Could the open second branch thereby be turning a mediocre instrument into one of higher quality? To consider this possibility, we conducted some numerical modelling.

### 4.2 Numerical modelling

To understand qualitatively how these features in $Z_{IN}(f)$ arise, it is useful to undertake some numerical modelling, although the model used in figure 2 very substantially underestimates the complex bore of a traditional instrument. The upper curve in figure 5 shows $Z_D(f)$, the input impedance for tube A if the extra tube (in this case tube B) were absent or blocked off at the junction. This configuration would correspond approximately to a conventional didjeridu. $Z_D(f)$ shows the expected series of maxima with a gradual decrease in magnitude with increasing frequency. There is also some modulation of the envelope of the curve due to higher frequency resonances in the shorter, final section of larger diameter (tube C).

![Figure 4](image)

**Figure 4.** The measured acoustic impedance spectral data of figure 2 shown on an expanded scale for low frequencies. The vertical arrows indicate the frequencies of the musical notes played on the instrument by one of the investigators.
When tube B is present, it introduces an additional impedance \( Z_B \) in parallel with \( Z_C \), the impedance of tube C from the junction to the external radiation field. We define \( Z_P \) as the parallel combination of \( Z_B \) in parallel with \( Z_C \). The impedance \( Z_C \) is less than \( Z_B \) at low frequencies and, because ducts in parallel add admittances rather than impedances, the only features of tube B that will appear in \( Z_P \) correspond to the minima in \( Z_B \) (see figure 6). The effect of these minima is to produce additional, small maxima in \( Z_{IN} \).

If the end of tube B is open, \( Z_B \) will be roughly similar to \( Z_D \), providing that \( L_B \) is not too different from \( L_A + L_C \), and consequently their minima will occur at similar frequencies. These minima in \( Z_B \) will produce minima in \( Z_P \) that in turn produce maxima in \( Z_{IN} \) around the frequencies where minima would occur in the absence of tube B – see figure 6.

Figure 6 shows that, if the end of tube B is closed, \( Z_B \) is almost the inverse of \( Z_B \) when open (it is not exactly the inverse because there is also a radiation impedance present when the tube is open). In this case, minima in \( Z_B \) occur at frequencies that correspond approximately to the maxima in \( Z_D \). They will thus produce minima in \( Z_P \) that in turn produce maxima in \( Z_{IN} \) around the frequencies where maxima would occur in the absence of tube B – see figure 6. This will effectively produce notches in the maxima of \( Z_D \) producing the pairs of adjacent maxima – see figure 6.

Figure 5. The calculated acoustic input impedance \( Z_{IN} \) of the model shown in figure 2. The upper curve was calculated with tube B blocked off at the junction and corresponds to a conventional didjeridu. The lower curves show the influence of tube B.
The exact dependence of $Z_{IN}$ upon frequency will depend in a complicated way on the actual geometry of the forked didjeridu, particularly at high frequency. This is because the frequency dependent load produced by tube B will have a greater effect, at a given frequency, when there is a pressure maximum at the junction, and this will depend upon the location of the junction. Nevertheless, figure 3 shows that, under some circumstances, the addition of a parallel duct can reduce the magnitude of several sequential impedance peaks.

4.3 The sound produced by two players.

To a first approximation, a duct closed by a player’s lips behaves acoustically like a closed end. So figure 4 shows that the impedance peaks available for playing regimes are somewhat similar for the two players.

Figure 6. The calculated acoustic impedance of the model shown in figure 2. The left and right hand curves were calculated with the end of tube B open or closed respectively. The top curves show the impedance $Z_B$ of tube B alone as seen from the junction. The middle curves show the impedance $Z_P$ presented at the junction by tube B and tube C in parallel. The lower curves show the input impedance $Z_{IN}$ of the instrument when played at tube A. The dashed line on the lower curves shows the input impedance $Z_D$ if tube B were totally absent (i.e. blocked off at the junction).
A notable feature of the sound produced the didjeridu is the very wide range of heterodyne components produced when a single player vocalises during playing. Thus if the didjeridu plays a note at frequency $f$ while the player vocalises at a frequency $g$, the non–linearities present can produce frequency components at frequencies given by $nf \pm mg$, where $m$ and $n$ are integers, e.g. see Fig 11 of Tarnopolsky et al., 2006 [6]. Even without vocalisation, two players using pairs of the impedance peaks shown in Figure 4 can produce similar sets of heterodyne components. Two of the investigators found this possible, but somewhat difficult to control. The possible frequency components if two players play and vocalise simultaneously at four different frequencies are bewildering.

5. CONCLUSIONS

The additional mouthpiece on a forked didjeridu can allow a player to produce changes in pitch and timbre by using the heel of his hand to close it. These effects can be explained by the use of a simple numerical model. Under propitious conditions, the extra tube may improve the playing qualities, which suggests the possibility of 'tuning' the length of one side tube to improve the quality of an instrument.

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