LEARNING ACOUSTICS THROUGH THE BOUNDARY ELEMENT METHOD: AN INEXPENSIVE GRAPHICAL INTERFACE AND ASSOCIATED TUTORIALS

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ABSTRACT The Boundary Element Method (BBA) is a powerful tool which has become an important and useful numerical feedingies applied to problems incuracious, it is principally useful for an analysis goard radiation and acquire scarcing from prices. Numerous contracted BEAC codes with agriphed user incurfaces (UM) and much generates exist, however these are relatively expensive, which discourages their inter by usa familie institutions and smaller companies. The ABST is a state-endirensianal BEAC codes synable with products of relatively successive book, but the command the driven tenteries in efficient to fear and some mechanism to generate the much is required, in addition, there is a finished variability of satisfies the total minerial, so the spatial of BEAC through one and come mechanism to generate the much is required, in addition, there is a finished variability of satisfies the total minerial, so the spatial of BEAC through one and come mechanism to generate the much is required, in addition, there is a finished variability of satisfies the total and removal, and the spatial of BEAC through one and the spatial of BEAC thr

NOMENCLATURE o density

ρ density ω angular frequency

a source radius
 c speed of sound

c(x) position dependent constant p(x|x) free space Green's function

 $g(x_s|x)$ tree space Green's function k wavenumber

l duct length
n mode number

n mode number
n number of elements

n, number of nodes p pressure

radial distance time

position of the field point location of CHIEF point

position of the source specific acoustic impedance

INTRODUCTION

The acoustic Boundary Element Method (BEM) has been used to solve a wide range of practical problems in acoustics, such as the modelling of sound generated by loudspeakers (Pederson and Munch 2002, and Hodgson and Underwood 1997) or received by microphones (Juli 1993), the sound power radiated by a particular structure such as an engine valve cover (Ciskowski and Brebbia 1991) or a fan (von Eurott' 2000), and the sound scattered by hard structures (Morgans 2000).

Numerous commercial codes that implement acoustic BEM exist; however the licensing costs are prohibitively expensive for casual users, limiting the uptake of this technology by the wider acoustics community. There exist numerous non-commercial acoustic BEM codes, such as those associated with the book edited by Wu (2000). These source codes exist as pedagogical examples for teaching the basics of BEM at an advanced undergraduate or postgraduate tevel. They are written in Fortran 77 and are available the CD accompanying the book. They are fully featured and capable of solving practical problems (Morgans et al. 2004).

These non-commercial codes, whilst readily available with the purchase of the book, have not gained widespread use for a number of reasons: the interface is command file driven and requires access to some form of pre and postprocessor, and there is a limited availability of suitable tutorial material.

Thus there is a need for:

an easy to use, freely available interface to an

acoustic BEM code, and

a well written, step by step tutorial on the use of BEM to solve simple relevant acoustic problems.

In this paper, brief outlines of direct BEM theory, the Lethr3D BEM code and the foll per and postprocessor are presented. An outline of the Graphical User Interface (GUI), developed with GID to solve direct BEM problems using the Helm3D code, is given. Finally, the tutorial material and how it will be used to teach the user fundamental acoustic and BEM concents are described.

DIRECT BEM

The boundary element method is a general numerical method for solving the Helmholtz harmonic wave equation. The traditional (direct) approach to BEM is to numerically approximate the Kirchoff-Helmholtz (K-H) integral equation (Juhl 1993, Morgans et al. 2004, Koopmann and Fahnline 1997, and Pierce 1994):

$$c(x)p(x) = -\int_{s} i\rho\omega v_{n}(x_{s})g(x_{s} \mid x) + p(x_{s})\frac{\partial g(x_{s} \mid x)}{\partial n}ds$$
(1)

where c(x) is a position dependent constant (unity outside the volume of interest. 1/2 on the surface of the volume and zero inside the volume), p(x) is the complex pressure amplitude (with $e^{-i\alpha x}$ time dependence) at location x, $i = \sqrt{-1}$, ρ is the fluid density, ω is the angular frequency, $v_n(x_s)$ is the normal surface velocity at location x and g(x, |x) is the free space Green's function relating locations x and x.. The K-H equation can be derived from the Helmholtz equation using either physical arguments using monopoles and dipoles (Fahy 2001) or using vector calculus and Green's theorem (Koopmann and Fahnline 1997, and Fahy 2001). Equation (1) is the fundamental equation of direct BEM, and shows that the pressure at any point can be represented by the surface integral of a combination of monopoles (first term in the integral of Equation (1)) and dinoles (second term in the integral of Equation (1)) aligned with the surface normal. The monopole source strength is weighted by the product of density and surface acceleration and the dipole source strength is weighted by the surface pressure. Given a distribution of surface normal velocity (which is the boundary condition usually prescribed), once the surface pressure is found, the pressure field anywhere in the domain can be calculated.

Direct BEM can be used to solve the Helmholtz equation in either a bounded interior domain (interior problem) or an unbounded exterior domain (exterior problem). The surface pressure is found by discretising Equation (1) with n_i nodes and n_c elements similar to those used in FEA. If the field point is positioned at each surface node (or "collocated") then a series of n_c equations for the n_c surface pressures can be found for a given velocity distribution. The equations are generated by numerical integration over each element, and the integration technique used must be capable of dealing with the singularities found at the locations of the monopoles with the singularities found at the locations of the monopoles inverted using standard linear algebra techniques. Once the matrix is inverted, and the surface pressures known, the field pressures can be calculated.

There are a number of disadvantages to the direct BEM approach, if the K-1 mitegal equation is used to represent the sound field on the exterior of a finite volume, at the natural frequencies of the interior of the finite volume, the exterior problem breaks down and the matrix becomes ill-conditioned. This is well documented (Copley 1968) and many solutions have been attempted (Schenck 1968), and Burton and Miller 1971). The CHIEF method (Schenck 1968) is commonly used to overcome the interior natural frequency problem because of its simplicity. This technique solves an overdetermined system is simplicity. This technique solves an overdetermined system of the control of th

Another problem occurs when the two surfaces of interest are brought close together, resulting in "thin-shape breakdown" (Martinez 1991). This means that although some geometries are probably best represented with a thin surface, a direct BEM simulation may either be not possible, or the geometry must be enclosed in a lareer volume. Although the BEM is mathematically complex, once it has been implemented in a computer code the user is sometime and the complex of the complexity. The BEM formulation can be verified by compraison with analytical solutions, ensuring solutions, the three complexity of the complexity. The best complexity of the experimental data, ensuring that the equations are control to the user can then concentrate on generating the geometry and analytic boundary conditions.

HELM 3D

The direct BEM code used in this research is Helm 3D, a Fortran 77 implementation using linear triangular or quadrilateral elements. It is able to solve interior or exterior problems with a wide variety of applied boundary conditions. The code is available with the purchase of the accompanying book (Wu 2000). The code reads in the geometry, boundary conditions, filed points and CHIEF points from a text based input file, forms the BEM matrix equations and solves the matrix for the boundary unknown using least-squares routines. The sound pressure at user-specified points and the sound power and radiation efficiency for radiation problems are evaluated.

The code can currently only solve simple acoustic problems. There is currently no mechanism to solve a coupled vibroacoustics problem, where the acoustics can affect the vibration and vice versa.

GUI

GiD (http://gid.cimne.upc.os) is a general-purpose, fully featured finite element per and post proxXsor developed over a number of years by the International Centre for Numerical Methods in Engineering (CIMNE) in Barcelona, Spain. It has extensive geometry creation features as well as CAD import (IGES and others), supports the meshing of many different element types and the application of boundary conditions, and has a postprocxxxiing capability for viewing results. Figure 1 shows a representative our interfor meshed in GiD.

The academic version of this program is freely downloadable, the only restriction being limited to 700 3D elements. Fortunately for BEM, this is a reasonable size and many useful acoustic problems can be solved.



Figure 1. Car interior meshed using GiD.

GID is designed to be easily customised and exchange data with a variety of numerical analysis codes. There are mechanisms available to apply custom boundary conditions, material properties and solution controls to the model. Most of these solvers, including Itelm 4d, require some form of text file, ascending to the control of the control of the site as input. Gill completely wange the creation of the control of the control of the solver and interpretation of the postmecosine data, makine the overaction transacratent to the user.

The Helm3d GUI (graphical user interface) developed for his project is straightforward to install (installation instructions are included in the tutorial). Figure 2 shows the problem data dialogue box, which allows the user to specify most of the required inputs that control the simulation. These include the project title, the frequency range of interest, whether the problem is an internal or external problem, material properties such as density and speed of sound, the position of a field point (a "microphone" that can be placed anywhere in the domain), and the position of any required CHIEF point.

The boundary conditions that can be applied in Helm3d are a surface pressure (rarely used), a surface normal velocity or a surface normal impedance. These can be applied using the boundary conditions dialogue box, either to model surfaces, or directly to the surface mesh.



Figure 2. Problem data dialogue box.

An important requirement for a BEM code is control over surface normals. Each surface element has a positive "side", and it is imperative that the side is facing outwards for internal problems (cavities) and inwards for external problems. GiD has a mechanism of visualisation of surface normals, and it is easy to modify normal directions until all surfaces are pointing in the required direction. Figure 3 shows the car surfaces with dark grey positive and light grey negative. For this simulation the 4 light grey surfaces must be flipped in order to solve the internal BEM problem.

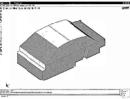


Figure 3. Surface normal visualisation.

The postprorscsing capabilities of GiD are extensive, and the results of a Helm3d calculation can be read and displayed easily. Figure 4 shows an example of a plot of pressure magnitude at 100 Hz over the interior of the 3 m long, 1.2 m high and 1.8 m wide car. A velocity excitation represents sound transmission through the engine firewall.

The GUI interface to Helm3d developed for this project is somewhat rudimentary, although it is sufficient to learn the BEM and acoustics. Future developments of the GUI might allow: multiple CHIEF points; multiple field points or even a field mesh that allows visualisation of the sound field away from the surface; or the inclusion of acoustic scattering from within the GUI.

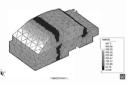


Figure 4. Pressure magnitude in a car interior (pressure in Pascals).

TUTORIALS

The tutorial guides the user through BEM modelling with eight problems, each introducing different aspects of:

• fundamental concepts in acoustics,

- BEM specific concepts, and
 - BEM specific concepts, and using the GiD-Helm3d interface.

The tutorial material comprises step-by-step instructions which explain how to input each model, apply boundary

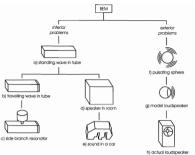


Figure 5. Breakdown of the tutorial problems.

conditions and postprocess the results. Comparisons with analytical solutions are given when possible. By the end of the tutorial, the user should have had an

introduction to these fundamental concepts in acousties:

• one-dimensional standing waves,

- one-dimensional travelling waves.
- impedance (sound absorbing) boundary conditions.
- modes in a rectangular room,
- modes in more complex spaces,
- one-dimensional spherical waves, sound radiation from a sphere, and
- sound radiation from a sphere, and
 sound radiation from more complex shapes.
- The user should understand these BEM specific concepts:
- advantages and disadvantages when compared to other techniques.
- interior versus exterior problems,
- element types,
 mesh size (6 elements per wavelength).
- non-uniqueness difficulty (CHIEF points),
- symmetry, and
 direction of normals
- direction of normal:

The user should also have a working knowledge of these GiD-Helm3d interface concepts:

- inputting the geometry into GiD directly,
- importing CAD data into GiD for meshing,
- flipping surface normals,
 meshing the geometry.
- mesning the geometry,
 applying boundary conditions.
- solving the problem through the GiD interface to Helm3d, and
- post-processing results through GiD.

Figure 5 shows the breakdown of the tutorials. Two application areas are addr^{CSSCd}: interior acoustics and external acoustic radiation. Simple problems with analytical solutions are introduced. The power of BEM is then demonstrated

INTERIOR PROBLEMS

through application to more realistic problems.

A simple model of a 1D standing wave in a rigid valled ut (Figure 5a) introduces the user to BEM through the very simple geometry of a long rectangle. Velocity boundary conditions, the required direction of normals and meching are introduced. How the accuracy of results can be affected by mesh resolution is also demonstrated. Results obtained from the numerical model are then compared to the analytical solution. An example of sound with a wavelengh identical to the duct length, resonating in a hard walled duct, is shown in Figure 6. A unit input velocity at the left end and zero velocity conditions elsewhere are assumed.



Figure 6. Standing wave in a duct at the SSSSnd theoretical resonance frequency of the duct (pressure in Pascals).

The resonance frequencies of the system are simply the resonances of an open-closed duct and are given by:

$$f_n = \frac{nc}{2l}$$
 (2)

where v is the mode number, c is the speed of sound and l is the length of the duct.

The analytical specific acoustic impedance at the excitation

 $Z_r = 0 - i\rho c \cot(kl)$

where $i=\sqrt{-1}$, ρ is the density of the medium and k is the wavenumber. The theoretical specific acoustic impedance and the BFM specific acoustic impedance (the ratio between the acoustic pressure and particle velocity) at the point of excitation are compared in Figure 7 as a function of frequency. The BFM is shown to be in good agreement with the theoretically determined values:

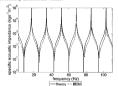


Figure 7. Harmonic response of an open-closed acoustic duct at the point of excitation.

The concept of impedance is introduced by the addition of absorption to the downstream end of the duct (Figures 5.b and 8), yielding a travelling plane wave, which is shown to have a very simple analytical solution.

The analytical pressure at any point in the duct is given by the equation:

$$p(x) = \rho c e^{-ikx}$$
(4)

where ξ is the distance from the point of excitation along the duct. As can be seen from Figure 9, the real and complex pressures of the travelling wave estimated using BEM agree well with the analytical solution.



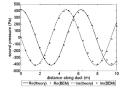


Figure 9. Sound pressure along the centre of one side of the duct.

A side branch resonator is then added (Figure S.c), and the analysis frequency is swept through resonance. The results of the analysis are used to show how the resonator adds impedance in parallel with that of the pipe, resulting in a suppression of tones close to the resonance frequency. An example of a meshed boundary element model of a duct with a side branch Helmholtz resonator is shown in Figure 10.



Figure 10. Mesh view of duct with side branch resonator.

A model of a speaker in the corner of a rigid walled room (Figure 5.4) includes the user to the excitation of modes in a 3D environment. Rectangular rooms with three different said dimensions are compared to those that have two or more identical dimensions. Various source shapes (of identical volume velocity) are also investigated, extending the user's understanding of room acoustics and BEM source modelling. An example of the excitation of from modes in two directions is shown in Figure 11. The room dimensions are 2.5 m a × 2 m to the properties of the control of the value with the longest dimension, and operates at a frequency of 68.5 Hz, corresponding to a wavelength of 5.

The final internal problem, the sound pressure in the interior of a car (Figures 4 and 5.e), is an example of how BEM can be applied to a practical 3D problem. Figure 4 shows the response within the interior of the car. Rigid wall boundary conditions are assumed. In practice the flexibility of the enclosing structure would need to be accounted for; however,



Figure 11. Pressure on wall of room containing sound source near one corner.

coupled problems such as this would require BEM codes far more complicated than the Helm3D code.

EXTERIOR PROBLEMS

The first exterior problem presented is the classical fundamental radiation problem of a pulsating sphere (Figure 5.). Key concepts covered are modelling symmetry and how this affects computational efficiency, appropriate direction of notice morphisms of the acternal problem and the use of CHIEF points in the interior to improve the condition number of the governing matrix. A meshed model of the half sphere (a symmetry boundary conditions is used) is shown in Figure 12.

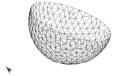


Figure 12. Mesh view of a pulsating sphere.

The analytical solution for the pressure produced by a pulsating sphere, which can be derived from the spherical wave equation, is:

$$p(r) = \left(\frac{a^2}{r}\right) \frac{i\rho\omega}{1 + ika} e^{-ik(r-a)}$$
(5)

where a is the sphere radius, r is the radius at which the pressure is being calculated and ω is the angular frequency. The characteristic eigenfrequencies of the sphere, which are the eigenfrequencies of the interior Dirichlet problem, are given by the equation:

$$\sin ka = 0$$
 (6)

Figure 13 shows the variation in surface pressure (r=a) with frequency for the pulsating sphere for an analytical solution, and BEM calculations with no CHIEF point, a CHIEF point at the centre of the sphere and a CHIEF point at half the radius.

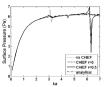


Figure 13. Surface pressure of a pulsating sphere

The BEM solution with no CHIEF point shows poor agreement with the analytical solution at $ka=\pi$ and $ka=2\pi$. where k is the wavenumber and α is the radius of the source. This is due to poor conditioning of the matrix. The placement of a CHIEF point at r/a = 0.5, where r is the radial location from the centre of the sphere, ameliorates the problem at ka=n: however, noor agreement at $ka=2\pi$ still occurs due to the CHIEF point being on the interior nodal surface corresponding to the characteristic eigenfrequency ka=2π, meaning that this resonance cannot be cancelled. Placing the CHIEF point at the sphere centre ensures that it does not lie on a nodal surface. The resulting solution is therefore in good agreement with the analytical solution. When using BEM to analyse more complex geometries, the user generally has no prior knowledge of the optimal CHIEF point location, and therefore multiple CHIEF points randomly distributed within the volume are used. The condition number of the matrix will also give an indication of whether there are any interior resonance problems.

A spherical volume with an external velocity over a proportion of its surface is presented as a simplified moder of a loudspeaker in a rigid walled box (Figure Sy). Comparison of results at different frequencies is used to show that radiation is inefficient at low frequencies. The example shows how a BEM of a problem with simplified geometry can be used to most own the simplified geometry can be used to make a similar pattern of behaviour. Application of the external Brainsirial pattern of benoviour. Application of the external Brainsirial pattern of benoviour. Application of the external Brainsirial pattern of benoviour. Application of the external Brainsirial pattern of benoviour application of the external Brainsirial pattern of benoviour.

CONCLUSIONS

This paper describes: a freely available interface that has been developed between GiD and Helm3d; and tutorial material describing some fundamental acoustic problems and how they would be solved with BEM using the newly developed interface. It is hoped that the resulting practical and freely available introduction to BEM will be the basis for and freely available introduction to BEM will be the basis for the property of the property of the property of the colved! as for a series of lectures in acoustics comes at some universities. The proposed greater availability of the code and tutorial will accelerate the uptake of BEM by the wider acoustics community, including members of the acoustical society as well as practicing acoustic engineers.

For further information please visit

http://www.mecheng.adelaide.edu.au/anvc/helm3d.html

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